Structure of North American mantle constrained by simultaneous inversion of multiple-frequency SH, SS, and Love waves

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[1] We simultaneously invert for the velocity and attenuation structure of the North American mantle from a mixed data set: SH wave traveltime and amplitude anomalies, SS wave differential traveltime anomalies, and Love wave fundamental mode phase delays. All data are measured for multiple frequency bands, and finite frequency sensitivity kernels are used to explain the observations. In the resulting SH velocity model, a lower mantle plume is observed to originate at about 1500 km depth beneath the Yellowstone area, tilting about 40° from vertical. The plume rises up through a gap in the subducting Farallon slab. The SH velocity model confirms high-level segmentation of the Farallon slab, which was observed in the recent P velocity model. Attenuation structure is resolvable in the upper mantle and transition zone; in estimating it, we correct for focusing. High-correlation coefficients between $\delta \ln V_S$ and $\delta \ln Q_S$ under the central and eastern United States suggest one main physical source, most likely temperature. The smaller correlation coefficients and larger slopes of the $\delta \ln Q_S - \delta \ln V_S$ relationship under the western United States suggest an influence of nonthermal factors such as the existence of water and partial melt. Finally, we analyze the influence of the different components of our data set. The addition of Love wave phase delays helps to improve the resolution of both velocity and attenuation, and the effect is noticeable even in the lower mantle.


1. Introduction

[2] Recent progress in high-resolution tomography has led to a clearer view of subduction history and slab geometry: subducted slabs may be torn apart and segmented [Nolet, 2009]. The Farallon slab shows evidence of segmentation under North America. Various hypotheses for the deformation of the Farallon slab have been proposed, including “slab buckling” [Humphreys, 1995] and “slab roll back” followed by detachment [van der Lee and Nolet, 1997a]. Sigloch et al. [2008] present the clearest evidence so far for high-level segmentation of the Farallon slab, an observation that was supported by P and S wave studies by Roth et al. [2008], Burdick et al. [2009], Tian et al. [2009], Xue and Allen [2010], and Obrebski et al. [2010]. The way in which the Farallon slab broke up into fragments has direct effects on subduction dynamics, by controlling the width of the slab and thus the trench migration rates [Schellart et al., 2007] which in turn influences the ability of the slab to enter the lower mantle [Goes et al., 2008]. The observed tears in the Farallon slab allow for mantle upwellings and thus may contribute to explain the widespread and complex patterns of magmatism in the western United States [Smith and Luedke, 1984]. Tomographic studies of the mantle beneath North America are necessary to examine how the Farallon slab deformed and fragmented. Our study serves this purpose.

[3] Comparisons between attenuation and velocity heterogeneities provide further insight into the physical state of the mantle, because different physical sources for mantle heterogeneity, such as temperature [e.g., Karato, 1993; Jackson et al., 2002], water content [e.g., Karato, 2006], partial melt [e.g., Jackson et al., 2004; Faul et al., 2004], chemical composition [e.g., Lee, 2003], and grain size [e.g., Faul and Jackson, 2005], give different attenuation-velocity relationships. There have been few tomographic studies on the attenuation structure of North American mantle.

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Lawrence et al. [2006] mapped the two-dimensional $P$ and $S$ $t^*$ residuals under North America but with no depth constraints. Yang and Forsyth [2008] simultaneously inverted for one-dimensional $V_S$ and $Q_m$ structure of the upper mantle beneath southern California. Hwang et al. [2009] estimated the two-dimensional $P$ wave $t^*$ structure under North America with no depth constraints. The first joint inversion for three-dimensional $V_P$ and $Q_P$ structure under North America was conducted by Sigloch et al. [2008]. The first joint inversion for three-dimensional $V_S$ and $Q_S$ structure under the western United States was carried out by Tian et al. [2009], using multiple-frequency $SH$ wave traveltimes and amplitudes.

The current study extends the work by Tian et al. [2009] by including $SS$ wave delays and Love wave phase data and imaging the mantle under North America. We simultaneously estimate the $SH$ wave velocity and attenuation structure under North America, taking advantage of three recent developments in seismology: (1) the large volume of data provided by the USArray which has densely sampled the western United States; (2) finite frequency sensitivity theory and the fast computation of the sensitivity kernels for body wave traveltimes [Dahlen et al., 2000], focusing effects [Dahlen and Baig, 2002], attenuation [Nolet, 2008, section 8.5], and surface waves [Zhou et al., 2004]; and (3) accurate techniques to measure frequency-dependent body wave traveltimes and amplitudes [Sigloch and Nolet, 2006] and surface wave phase delays [Laske and Masters, 1996]. The velocity model is used to study the mantle dynamics under North America. The velocity and attenuation models are compared to gain insight into the sources of mantle heterogeneities. Effects of adding new types of data, especially the Love wave phase delays, are also investigated.

2. The Data Set

[5] We use a mixed data set consisting of four different types of data, which are all measured at multiple frequencies from the transverse component: $SH$ wave traveltime anomalies, $SH$ wave amplitude anomalies, $SS$ wave differential traveltime anomalies, and Love wave fundamental mode phase delays. This data set is an extension of the $SH$ data set built by Tian et al. [2009], to which we add (1) Love wave phase delays, (2) $SS$ wave differential delays, and (3) more $SH$ wave measurements from most recent USArray stations. Love waves are particularly helpful. They provide the depth resolution which body waves lack because
in the shallow region the teleseismic body wave paths are almost vertical. SS waves help to improve the resolution with reflection points covering regions not sampled by direct SH waves.

2.1. SH Wave Traveltime and Amplitude Anomalies

We construct a global data set of SH wave traveltime anomalies

$$
\delta T_S = T_{S}^{\text{obs}} - T_{S}^{\text{pre}}
$$

and amplitude anomalies

$$
\delta \ln A_S = A_{S}^{\text{obs}} / A_{S}^{\text{pre}} - 1
$$

(with "obs" for observed and "pre" for predicted data) in five frequency bands with center periods of 40, 20, 10, 5, and 2.5 s, respectively (see Tian et al. [2009] for the passband filter responses). The measurements are obtained through cross correlation, using the technique developed by Sigloch and Nolet [2006]. These measurements are deviations from predictions computed for the IASP91 $V_S$ model [Kennett and Engdahl, 1991] extended with the PREM $Q_S$ model [Dziewonski and Anderson, 1981]. Details of how to construct the data set and discussions of the frequency dependence and spatial distribution of the data set are described by Tian et al. [2009]. In this paper, we update the SH wave data set with more recent USArray data until October 2008. The current SH data set consists of 26,296 wave paths, producing 98,371 acceptable traveltime measurements in the five frequency bands and 74,665 acceptable amplitude measurements in the three low-frequency bands. For an idea of the SH data coverage in North America, see Figures 5c–5e and 6c–6e.

2.2. SS Wave Differential Traveltime Anomalies

We measure the SS wave differential traveltime anomalies

$$
\delta(T_{SS} - T_S) = (T_{SS} - T_S)^{\text{obs}} - (T_{SS} - T_S)^{\text{pre}}
$$

in the same five frequency bands as for SH waves. The observed differential traveltimes $(T_{SS} - T_S)^{\text{obs}}$ are measured by cross-correlating the observed SS waveform with the predicted SS waveform. The predicted SS waveform is computed by Hilbert transforming the observed SH waveform, applying the attenuation operator to account for the difference in attenuation along the SS and SH paths, and multiplication by $-1$ to account for the reflection at the free surface. Both the observed and predicted SS waveforms are filtered in each of the five frequency bands, and the cross correlation is done in each band.

We measure any SS wave that has a corresponding acceptable measurement of $\delta T_S$ (see section 2.1) and that has an epicentral distance between 60° and 88°. The quality of acceptable $\delta T_S$ guarantees reliable estimates of the SH wave window and source depth, which are used to compute the predicted SS waveform. The lower limit of 60° is to exclude triplications of SS, and the upper limit of 88° is to exclude D" and CMB diffracted SH waves [Paulssen and Stutzmann, 1996]. Measurements are deemed acceptable by visual
inspection of the waveform fits after cross correlation. We impose a lower limit of 0.9 on the cross-correlation coefficient. The two high-frequency bands (with center periods of 5 s and 2.5 s) are not used for tomography because the \((TSS − TS)_{obs}\) uncertainty estimated from pairs of closely located events is much larger in these two bands (\(\sim 1.8\) s) than in the other frequency bands (\(\sim 0.8\) s). The final SS wave data set consists of 18,919 measurements from 8270 wave paths in three frequency bands (with center periods of 40 s, 20 s, and 10 s). The SS data coverage in North America is shown in Figures 5b and 6b.

To examine the consistency of the measurements, Figure 2 plots \(\delta(TSS − TS)\) at each reflection point for unfiltered (“broadband”) data, which reflects anomalies in the shallow subsurface beneath the reflection point. The map shows distinct large-scale patterns, and they correlate with tectonic structure. For example, negative anomalies at the Canadian shield and the Siberian shield, positive anomalies in western North America and western Central America. The patterns are similar to those observed by Woodward and Masters [1991] and Reid et al. [2001].

After applying crustal, ellipticity, and elevation corrections, the histogram of SS differential delays in each frequency band is plotted in Figures 3a–3c. The histograms are skewed toward negative anomalies. One possible cause of this asymmetry is that more reflection points hit the region with fast shallow structure (see Figure 2). Figure 3d examines the dispersion of SS differential delays with respect to the lowest-frequency band. The dispersion is of the order of 1 s, which is of the same order as the uncertainty in SS differential delays. If the dispersion is completely due to random noise, one expects to observe a zero median and the same standard deviation in the 20 and 10 s bands. The nonzero medians in both bands and the clear trend of larger dispersion with increasing frequency difference suggest that the observed dispersion is at least partially due to the finite frequency effect, though at low-frequency crustal effects may play a role [Ritsema et al., 2009].

2.3. Love Wave Fundamental Mode Phase Delays

For Love waves, we use the fundamental mode minor arc phase delays, measured at 11 frequencies (5, 6, 7,
histogram of Love wave relative phase delays $\delta \phi/\phi$ at 11 frequencies (5, 6, 7, ..., 15 mHz) used in this study, after applying crustal corrections.

... 15 mHz) with a multitaper technique [Laske and Masters, 1996]. This data set consists of 19,485 phase delays from 1778 wave paths. It is part of the global surface wave data set used by Zhou et al. [2006]. Figures 5a and 6a show the Love wave data coverage in North America. The original phase delays used by Zhou et al. [2006] are for the reference model 1066A [Gilbert and Dziewonski, 1975]. To be consistent with the body waves, the phase delays are corrected to be for the reference model IASP91 [Kennett and Engdahl, 1991]. After crustal corrections, the histograms of the relative phase delays $\delta \ln \phi = \delta \phi/\phi$ are plotted in Figure 4.

2.4. Data Corrections and Uncertainties

[13] For body waves, when computing $SH$ and SS traveltimes, the effects of ellipticity, crustal structure, and station elevations are taken into account [Tian et al., 2007a]. The crustal corrections are computed using ray theory and the three-dimensional crust model CRUST2.0 [Bassin et al., 2000]. According to Ritsema et al. [2009] and Obayashi et al. [2004], the crustal correction difference $\Delta (b_L)$ between ray theoretical and finite frequency calculations are not negligible for long-period waves. This is a potential source of uncertainties for $SH$ and SS traveltimes. Specifically, for $SH$ waves, Ritsema et al. [2009] show that the ratio between $\Delta (b_L)$ and the RMS of measured traveltime anomalies is 0.144, 0.146, and 0.184 for 40, 20, and 10 s periods, respectively. For SS waves, the ratio is 0.069, 0.110, and 0.055 for 40, 20, and 10 s period, respectively. The uncertainties in $\delta T_S$, $\delta \ln A_S$, and $\delta (T_{SS} - T_S)$ are estimated based on (1) difference between two measurements from two closely located events at the same station; (2) variation of one measurement with cross-correlation window length; and (3) quality of the waveform fit. As a result, the $\delta T_S$ uncertainties range from 0.6 s to 1.2 s, the $\delta \ln A_S$ uncertainties range from 0.12 to 0.22 (0.98 to 1.73 dB or $-2.16$ to $-1.11$ dB), and the $\delta (T_{SS} - T_S)$ uncertainties range from 1.1 to 1.7 s.

[14] For Love waves, the crustal structure has a very large effect on phase delays [e.g., Zhou et al. 2006]. Crustal corrections are computed using ray theory and the model CRUST2.0 [Bassin et al., 2000], and are applied to the phase delay measurements before inversion. We adopt the phase delay uncertainties estimated by Zhou et al. [2006] based on pairs of closely located events, and slightly adjust them in order to control the relative importance of different data types in the joint inversion. The uncertainty for the relative phase delay $\delta \phi/\phi$ ranges from 0.74% to 0.93%. Regional crustal models in the western United States have been developed based upon receiver function analysis and $Pn$ tomography of USArray data, and discrepancies exist among models developed by different research groups [e.g., Wilson et al., 2010; Buehler and Shearer, 2010]. However, details in regional crustal structure do not have significant effects on Love wave phase delays at the periods we are interested in. For example, a 5 km difference in crustal thickness over a propagation distance of 40° would introduce a $\delta \phi/\phi$ difference of less than 0.22% at 5 mHz frequency and a $\delta \phi/\phi$ difference of less than 0.59% at 15 mHz frequency. Both are smaller than the estimated uncertainty of $\delta \phi/\phi$.

3. The Joint Finite Frequency Tomographic System

3.1. The Continuous Linear System

[15] In finite frequency tomography, the linear inverse problem takes four forms corresponding to our four data types:

[16] 1. For $SH$ wave traveltime anomalies, the linear inverse problem is

$$
\delta T_S(s(\omega)) = \int \int K_{T_S}^T(s(\omega), R) \delta \ln V_S(R) \, d^2R + \delta T_0 + \delta X_0 \cdot \frac{\partial}{\partial V_S}X_0,
$$

with $\delta \ln V_S$ representing velocity heterogeneities, and the sensitivity kernel $K_{T_S}^T$ describing how the velocity heterogeneity affects $SH$ wave traveltimes [Dahlen et al., 2000]. Here $s(\omega)$ is the frequency content of the observed waveform that is used to measure $\delta T_S$. For our data set, we assume that this is equal to the frequency response of the passband filter. The last two terms are correction terms: $\delta T_0$ represents the origin time correction, vector $\delta X_0$ represents the hypocenter correction, and $\left(\frac{\partial}{\partial V_S}\right)X_0$ represents the slowness vector at hypocenter $X_0$.

[17] 2. For $SH$ wave amplitude anomalies, the linear inverse problem is

$$
\delta \ln A_S(s(\omega)) = \int \int K_{\delta A}^A(s(\omega), R) \delta \ln V_S(R) \, d^2R + \delta \ln A_0 + \delta \ln A_0
$$

Here $\delta \ln A_0$ represents attenuation heterogeneities. The sensitivity kernel $K_{\delta A}^A$ describes how the attenuation heterogeneity affects $SH$ wave amplitudes [Dahlen and Baig, 2002], and $K_{\delta A}^A$ describes how the attenuation heterogeneity affects $SH$ wave amplitudes [Nolet, 2008, Section 8.5]. $\delta \ln A_0$ is the source correction term accounting for the scalar moment errors and the uncertainty in source time function scaling in
the station correction term accounting for sediment effects and adjustment of the instrument magnification.

For SS wave differential traveltime anomalies, the linear inverse problem is

$$\delta(T_{SS} - T_{S})(s(\omega)) = \int \int (K_{V}^{TS}(s(\omega), R) - K_{V}^{TS}(s(\omega), R)) \delta\ln V_{S}(R) \, d^{3}R,$$

with $K_{V}^{TS}$ and $K_{V}^{TS}$ representing the SS and SH travelt ime-velocity sensitivities, respectively [Dahlen et al., 2000].

For Love wave phase delays, the linear inverse problem is

$$\delta\ln \phi(\omega) = \int \int K_{V}^{\omega}(\omega, R) \delta\ln V_{S}(R) \, d^{3}R + c \frac{\delta T_{0}}{\Delta}.$$

The sensitivity kernel $K_{V}^{\omega}$ describes how the velocity heterogeneity affects Love wave phase delays [Zhou et al., 2004], and $\omega$ is the angular frequency at which $\delta\ln \phi$ is measured. In the last term, $\delta T_{0}$ is the origin time correction, $c$ is the phase velocity in km/s, and $\Delta$ is the epicentral distance in km.

### 3.2. The Discrete Linear System

We use a model parameterization in the form of a tetrahedral mesh with linear interpolation in between grid nodes. The general philosophy of adaptive tetrahedral meshing is described by Nolet [2008, section 12.2]. Here we use the same tetrahedral mesh as in the work by Sigloch et al. [2008] and Tian et al. [2009]. Beneath the United States, the grid spacing of the mesh is about 70 km in the upper mantle, and increases to roughly 200 km at 660 km depth. Outside of the United States, the grid spacing is about 200 km in the upper mantle and transition zone. Below 660 km, the grid spacing increases linearly to about 300 km at 2000 km depth. The mesh is produced with the Matlab software distmesh developed by Persson and Strang [2004].

[21] With source and receiver correction terms and regularization, the complete discrete linear system of the tomographic problem can be written as

$$\begin{bmatrix}
K_{V}^{T_{S}} & 0 & K_{C}^{T_{S}} & 0 & 0 \\
K_{V}^{A_{S}} & K_{C}^{A_{S}} & 0 & K_{C}^{A_{S}} & 0 \\
K_{V}^{T_{SS}} - K_{V}^{T_{S}} & 0 & 0 & 0 & 0 \\
K_{V}^{\omega} & 0 & 0 & 0 & K_{C}^{\omega} \\
\epsilon_{1} \omega W & 0 & 0 & 0 & 0 \\
0 & \epsilon_{1} \omega W & 0 & 0 & 0 \\
0 & 0 & \epsilon_{1} \omega W & 0 & 0 \\
0 & 0 & 0 & \epsilon_{1} \omega W & 0 \\
\epsilon_{2} \omega W & 0 & 0 & 0 & 0 \\
0 & \epsilon_{2} \omega W & 0 & 0 & 0
\end{bmatrix}
\begin{bmatrix}
\delta\ln V_{S} \\
\delta\ln A_{S} \\
\delta(T_{SS} - T_{S}) \\
\delta\ln \phi \\
0 \\
0 \\
0 \\
0 \\
0 \\
0 \\
0 \\
0
\end{bmatrix} = \begin{bmatrix}
\delta T_{S} \\
\delta\ln Q_{S}^{1} \\
C_{SS}^{T_{S}} \\
C_{SS}^{A_{S}} \\
C_{SS}^{\omega} \\
0 \\
0 \\
0 \\
0 \\
0
\end{bmatrix}.$$

The first four rows correspond to equations (4)-(7). The vector on the right-hand side contains in sequence the four types of data, as described in section 2. On the left-hand
The kernel density (see equation (9)) for the five sensitivity kernels in equation (8) at 600 km depth. The heading indicates the kernel type. (a) For Love wave kernels and (b) for SS wave kernels. (c and d) For SH wave velocity kernels. (e) For SH wave attenuation kernels.

Figure 6. The kernel density (see equation (9)) for the five sensitivity kernels in equation (8) at 600 km depth. The heading indicates the kernel type. (a) For Love wave kernels and (b) for SS wave kernels. (c and d) For SH wave velocity kernels. (e) For SH wave attenuation kernels.

side, besides the velocity and attenuation heterogeneities, the model vector includes various correction terms: $C^{TS}$ represents hypocenter and origin time corrections for SH wave traveltimes (see equation (4)); $C^{SS}$ represents receiver and source corrections for SH wave amplitudes (see equation (5)); $C^o$ represents origin time corrections for Love wave phase delays (see equation (7)). The body wave finite frequency sensitivity kernels $K^T_s$, $K^T_v$, $K^Q_s$, $K^Q_v$ are computed using the software by Tian et al. [2007a, 2007b]. The Love wave finite frequency sensitivity kernels $K^L_v$ are computed using the software by Zhou et al. [2006]. $W$ is a diagonal weighting matrix, with its diagonal element proportional to the tetrahedral volume associated with the corresponding grid point, and $c_1$ is the norm damping parameter. $R$ is the Laplacian roughening operator [Nolet, 2008, section 14.5], and $c_2$ is the smoothing parameter. Equation (8) shows that velocity and attenuation have coupled effects on SH wave amplitudes, and SS and Love waves provide extra independent constraints on velocity. Our joint inversion interprets these data simultaneously.

As a measure of how strongly a particular tetrahedral volume in the Earth is sensed by the combined set of kernels, we compute the “kernel density,” defined as

$$D = \frac{\sum_j K_{ij}}{CV_j},$$

where $K$ stands for the tomographic matrices in equation (8), summation $i$ is over all data, $V_j$ is the average volume of the tetrahedron containing grid point $j$, and $C$ is a scaling constant such that the maximum $D_j$ is 1. The factor $1/V_j$ removes the effect of nonuniform grid spacing. Figures 5 and 6 plot $\log(D_j)$ for all the five sensitivity kernels in equation (8), at 100 and 600 km depth, respectively. Figures 5e–5e and 6c–6e show the kernel densities for SH waves. The dense coverage of the USArray is reflected in the large values of SH wave kernel densities in the western United States. For SH wave amplitudes, with the same ray coverage, the sensitivity to attenuation is about 1.5 orders of magnitude weaker than that to velocity. As we go deeper, the body wave sensitivity becomes wider although the strength slightly decreases near the geometrical rays. Figures 5a and 6a show that Love wave sensitivity is concentrated near the surface. Love and SS waves provide constraints on SH velocity outside of the U.S. region, where SH waves have poor coverage. Within the U.S. region, the Love wave and SS wave sensitivity is at least 1 order of magnitude smaller than that of SH waves, because of the small number of measurements for Love and SS waves. Nonetheless, they provide extra constraints independent of SH waves: Love waves are more sensitive to vertical gradients in velocity than SH waves.

### 3.3. The Inversion Scheme

[23] The joint linear system (8) has four different types of data with different orders of magnitude. Following a Bayesian philosophy [Nolet, 2008, section 14.5], we scale the data with their estimated measurement uncertainties (see section 2.4) and scale the model parameters with their “prior uncertainties,” which are estimated from results of existing tomographic studies. The model parameter prior uncertainties used in the final inversion are 0.01 for $\delta\ln V_s$, 0.2 for $\delta\ln Q_s$, 30 km for SH wave hypocenter corrections, 1 s for SH wave origin time corrections, 0.1 for SH wave amplitude event corrections, 0.15 for SH wave amplitude station corrections, and 1 s for phase delay origin time corrections. These estimates of both data and model uncertainties carry a subjective uncertainty and were in effect slightly adjusted within their margin of error as we gained experience with the data compatibilities during early inversion runs. Before inversion, the data and model parameters in equation (8) are divided by their uncertainties, and
Figure 7. Trade-off curve for velocity (circles) and attenuation (asterisks) models. (left) Trade-off between fitting the data and norm damping. (right) Trade-off between fitting the data and smoothing the model. The term $\chi^2/N$ is defined by equation (10), $m$ is the model vector $\delta\ln V_S$ or $\delta\ln Q^{-1}_S$ in equation (8), $R$ is the Laplacian roughening operator [Nolet, 2008, section 14.5], and verticals represent the L2 norm. Different points on the same curve correspond to different values of $c_1$ or $c_2$ in equation (8). The dotted line indicates the preferred model with $\chi^2/N = 0.928$.

Figure 8. Great circle cross sections of the subduction system under North America. The black dot and $0^\circ$ represent the midpoint of the great circle arc. In the map views, green lines delineate tectonic boundaries, dotted black lines delineate political boundaries, and the depth is indicated at the bottom left corner. In the cross-section views, the 410 km and 660 km discontinuities are indicated, and each grid along the arc represents 1°. SW denotes the slab window south of the Mendocino Fracture Zone, where no subduction exists. Cross section AA’ shows the two separate subduction systems: the younger one in the west ($S_0$, $S_1$, $S_2$) and the older one in the east ($F_1$, $F_2$); $C$ denotes the craton. Cross section BB’ shows that $F_1$ lies above $S_2$ and $N_2$. Labels $S_1$, $N_1$, $S_2$, $N_2$, $F_1$, $F_2$ identify the same structure as in the work by Sigloch et al. [2008].
The squared misfit of the observed data to the values predicted by equation (8) is given in the auxiliary material in Figures S4–S6 (right).

### 4. The SH Velocity Model of the Mantle Beneath North America

In this section, we discuss several interesting features of our SH velocity model of the mantle, which is derived from the IASP91 S velocity model [Kennett and Engdahl, 1991]. A complete catalog of the velocity maps is given in the auxiliary material in Figures S4–S6 (right).

#### 4.1. Subduction

The fast velocity anomalies in our model confirms the two-stage subduction under North America and the existence of tears in the Farallon slab observed by Sigloch et al. [2008]. Figure 8 shows the whole subduction system under North America. Figures 9 and 10 show the subduction under the western United States and the tearing of the slab. To facilitate comparison with the earlier P wave inversions, we use the same notation (S1, N1, S2, N2, F1, F2, SG) as Sigloch et al. [2008] to identify anomalies.

Fast anomalies are observed at 100–200 km depth under the Cascades (Figure S4, right; S0, N0 in Figures 9 and 10), indicating the most recently subducted Juan de Fuca Plate. It is subducting at a steep angle (S0 in Figure 8, AA'). The Juan de Fuca slab continues eastward, penetrating the transition zone (S1, N1 in Figures 8–10) and reaching the lower mantle (S2, N2 in Figures 8 and 9). Under the western United States down to ~800 km depth, no large fast anomaly is observed south of ~37°N (SW in Figures 8–10), which is the present Mendocino edge of the Juan de Fuca slab. This region with absence of subduction is known as the slab window, produced by the breakup and movement of the Farallon slab in the last ~28 Myr [Atwater and Stock, 1998]. Although Schmandt and Humphreys [2010a] found small-scale high-velocity anomalies possibly representing the slab coming to rest in the transition zone, our tomographic image indicates that the last large (~600 km) piece of the Farallon plate south of the Mendocino Triple Junction has sunk to at least 900 km depth. If the slab window formed at ~28 Ma [Atwater and Stock, 1998], this implies a vertical sinking
rate of 3.2 cm/yr, which is comparable to the speed of the Farallon plate at \( \sim 28 \) Ma [Engebretson et al., 1985].

[29] Under eastern North America, large volumes of fast anomalies (Figures S5 and S6, right; F1, F2 in Figure 8) are observed parallel to the young Juan de Fuca slab described above. They extend as far south as at least 25\(^\circ\)N, occupying the mantle beneath eastern North America down to at least 1400 km. This probably represents the ancient Farallon slab, and it is well separated from the Juan de Fuca slab, as can be seen from Figure 8: the western tip of F1 is riding above the eastern tips of S2 and N2 with a gap in between. The coexistence of the western and eastern subduction systems was first observed by Sigloch et al. [2008] and interpreted in terms of a big break at 50–40 Ma between F1 and S1. Consistent with their \( V_p \) model, we observe a flat F1 in the transition zone (Figure 8, AA') and a relatively steeper subduction angle of S1, which makes it easier for S1 to penetrate the transition zone.

[30] Taking advantage of the dense USAArray coverage, we are able to obtain a high resolution under the western United States and thus to study the detailed structure of the Juan de Fuca slab. The most striking feature is the slab gap (SG in Figures 9 and 10), which is a continuous 1600 km long trail void of fast anomalies and which divides the Juan de Fuca slab into a northern part (N0, N1, N2) and a southern part (S0, S1, S2). It starts at \( \sim 120 \) km depth near (45\(^\circ\)N, 238\(^\circ\)E), extends northeastward as it sinks deeper, and ends at \( \sim 800 \) km depth near (47\(^\circ\)N, 254\(^\circ\)E) (Figure S5, right, 800 km). Because there is no surface evidence showing the absence of subduction near (45\(^\circ\)N, 238\(^\circ\)E), the slab gap is more likely to have formed at \( \sim 120 \) km depth rather than at surface. We exclude the kinematic segmentation of the monolithic Farallon plate starting at \( \sim 30 \) Ma as the cause of the slab gap.
Most of this breakup of the Farallon plate occurred south of the Mendocino fracture zone, and the plate to the north (the Juan de Fuca plate) remained relatively intact [Atwater and Stock, 1998]. The slab gap revealed by our velocity model is inside the Juan de Fuca plate, so it is less likely to relate to the breakup of the monolithic Farallon plate. In addition, the slab gap reaches only 800 km depth, which suggests that the slab gap is younger than 30 Myr using the Farallon plate velocity by Engelder et al. [1985]. One possible cause of the slab gap could be the different subduction angles of the northern and southern parts of the Juan de Fuca plate, as shown in Figure 9. S1 enters the transition zone at a further east location than N1. Our velocity model shows that the subduction angle is ~60° (from surface) for S1, and ~70° for N1, and the thickness of S1 and N1 is ~70 km. A back-of-the-envelope calculation with this geometry suggests that S1 and N1 start to diverge (no overlap) at ~350 km, which is much deeper than the observed 120 km depth. This indicates that there are other causes contributing to the formation of the slab gap in the meantime, such as the interaction between the Yellowstone plume and the slab [Obrebski et al., 2010]. This slab gap was first discovered by Sigloch et al. [2008]. In their P velocity model, the slab gap extends longer (2500 km long) and deeper (1200 km deep) than in our model. The slab gap is also recognizable in other recent tomographic models [e.g., Obrebski et al., 2010; Schmandt and Humphreys, 2010b], although it is not discussed in these studies. The slab hole at shallow depth near 45°N under the Cascades that was observed in several recent studies [Roth et al., 2008; Tian et al., 2009; Burdick et al., 2009; Schmandt and Humphreys, 2010b] overlaps the upper tip of the slab gap, and thus is actually the top part of the slab gap.

[31] Evidence for more breaks or detachment of the slab is observed. At 700–1200 km depth, F2 is divided into two blob-like segments, along an east–west oriented break near ~40°N (Figure 8, AA′, and Figures S5 and S6, right). The $V_p$ model [Sigloch et al., 2008] shows a break at similar location and depth, but extending broader in the north–south direction and shorter in the east-west direction than in our $V_s$ model. S2 has a blob-like tail down to ~1600 km depth (Figure 8). Blob-like slabs in the lower mantle are also observed by seismic tomography under northern Kuril and Mariana [Fukao et al., 2009]. Such droplet-like slabs are modeled by numerical simulation with a large viscosity contrast across the 660 km discontinuity [Tagawa, 2007]. The droplet-like shape suggests strong deformation and perhaps detachment of the slab as it penetrates the 660 km discontinuity. The discontinuity between $S0(N0)$ and $S1(N1)$ (Figures 8, AA′, and 9) is the evidence of a further small-scale tear in the Juan de Fuca slab.

[32] Different hypotheses explaining the Farallon slab segmentation have been proposed to explain the post-Laramide magmatism in the western United States. The “slab buckling” model [Humphreys, 1995] predicts east-west oriented Farallon slab remnants. Anomalies S1 at ~40°N and N1 at ~47°N cannot be the north and south sides of the buckle which is now near 36°N. The “slab roll back and detachment” model [van der Lee and Nolet, 1997a] and the “two-stage subduction” model [Sigloch et al., 2008] predict north-south oriented Farallon slab remnants. Our $SH$ velocity model largely satisfies predictions from the subduction history of the Farallon slab proposed by Sigloch et al. [2008], such as the separation between anomalies S1 and F1, possibly resulting from a two stage subduction. Meanwhile we observe blob-like slab segments in the lower

Figure 11. Three-dimensional view of the plume-slab interaction system under Yellowstone and the eastern Snake River Plain, looking from the southwest. Red represents the isosurface of slow anomalies $\delta ln V_s = -0.5\%$, and blue represents the isosurface of fast anomalies $\delta ln V_s = +0.8\%$. The extent and geometry of the structure only change modestly as we shift the contour level between 0.5% and 0.8%. The green triangle represents the location of the Yellowstone Caldera. For slow anomalies above 660 km, only those under Yellowstone and the eastern Snake River Plain (40–46°N, 244–251°E) are displayed. Shallow fast anomalies that are not deemed to be subduction (e.g., the craton and the Colorado Plateau root) are not displayed. (a) Slow anomalies only. Under the eastern Snake River Plain, SR0 is in the upper mantle and SR2 is in the lower mantle. Under the Yellowstone Caldera, Y0 is in the upper mantle, Y1 is in the transition zone, and Y2 is in the lower mantle. (b) Superimposition of the fast anomalies on top of the slow anomalies. See Figure 9 for a description of the fast anomalies. Labels S1, N1, S2, N2, SG identify the same structure as in the work by Sigloch et al. [2008].
mantle and other smaller-scale slab tears, all indicating high-level segmentation of the Farallon slab.

33 The subduction-related features discussed above are reasonably well resolved, including the subduction under the Cascades (Figure S7, 100–200 km), the slab window (Figure S7, 100–800 km), the coexisting two subduction systems (Figure S8, AA'), the slab gap under the western United States (Figure S7, 200–800 km, and Figure S8, BB'), the break in F2 (Figure S7, 800–1200 km), the droplet-like geometry of S2 and F2 (Figure S8, AA'), and the discontinuity between S0 and S1 (Figure S8, AA').

4.2. The Yellowstone Plume

34 A strong slow anomaly (Y0) with large velocity gradient is observed under the Yellowstone Caldera (Figures 11a and 12). It has a diameter of ~200 km and reaches 200 km depth. Y0 connects to a 200 km wide slow anomaly (Y1) in the transition zone, which is centered at ~1° north of Y0 (Figure 12, AA'). To the southwest, Y0 abuts a belt of strong slow anomalies (SR0) under the eastern Snake River Plain (Figures 11a and 12, BB'). Down in the lower mantle, a plume-shaped 300 km wide conduit
(Y2) is observed with its top directly under Y1. The plume comes from south, tilting ∼40° from vertical, reaches as deep as 1500 km, but spreads out at 700–1100 km depth. Figure S8, CC′–DD′, shows that these velocity features are well resolved. A tilting plume under the Yellowstone that extends to the lower mantle is also observed by Obrebski et al. [2010] and Schmandt and Humphreys [2010b], but the plume comes from southwest in their models. The VS model of Obrebski et al. [2010] also shows that the plume spreads out at 600–900 km depth, a feature quite similar to that in our model. The image of a tilting whole mantle plume is quite different from previous tomographic images, especially in the lower mantle. Regional studies have shown an upper mantle plume from northwest with a smaller tilting angle [Yuan and Dueker, 2005; Waite et al., 2006], and other studies have revealed no plume-like features in the lower mantle [Montelli et al., 2006; Sigloch et al., 2008; Burdick et al., 2009].

The dimensions of Y0, Y1, and Y2 agree well with the expected plume radius from other studies [e.g., Montelli et al., 2004; Steinberger and Antretter, 2006]. The large southward tilting angle of Y2 is surprising because it would require a very strong mantle wind. Both Steinberger and O’Connell [1998] and Steinberger [2000] predict indeed a southward flow in the midmantle beneath the Yellowstone from numerical modeling of mantle flow. The spreading of SR2 can be explained either if the 660 km discontinuity acts as a barrier, as is sometimes observed for plumes [Nolet et al., 2006], or if the slab fragment S1 acts as a barrier for the uprising Y2 (Figure 11b). Y2 might have distorted in two ways in response to the barrier. Part of Y2 might have navigated its path around S1 and found its way up through the slab gap, and the other part of Y2 might have smeared southwestward along the base of S1 and formed SR2. Though much of this explanation is speculative, it is clear that we witness a complex interaction between upwellings and downwellings in this part of the mantle.

Much of Y0 and the eastern edge of SR0 have $\delta\ln V_S < -5\%$ above 120 km (Figure 12, BB′), and the peak anomaly is −7% at ∼50 km depth directly under the Yel-
lowstone Caldera. According to Cammarano et al. [2003] and Goes and Govers [2000], $\delta nV_S < -5\%$ requires a thermal anomaly of $\delta T > 250$ K, and the $-7\%$ velocity anomaly under the caldera requires an $\delta T$ of at least 350 K if it is a purely thermal effect. Tomographic studies with data from local transportable array experiments in the Yellowstone region [Schutt et al., 2008; Schmandt and Humphreys, 2010b] show even slower velocities under the Yellowstone Caldera and the eastern Snake River Plain, which indicate even higher temperatures. These high temperatures reach the solidus of peridotite at 50–100 km depth [Goes and van der Lee, 2002], and thus may cause partial melt in these regions, especially under the caldera. The partial melt is probably responsible for the magmatism in the Yellowstone and eastern Snake River Plain.

4.3. The New England Slow Anomaly

[37] Slow velocity anomalies up to $-3\%$ are observed under the New England Province from the surface to the bottom of the transition zone (Figure 13, AA'), and they are well resolved (Figure S8, EE'). Low velocity in this region down to the transition zone has been reported by van der Lee and Nolet [1997b] and has been confirmed by recent body wave studies [Sigloch, 2008; Burdick et al., 2009] and surface wave studies [Bedle and van der Lee, 2009]. According to Cammarano et al. [2003], under pure thermal effect, a $-3\%$ velocity anomaly at 100 km depth and a $-1\%$ velocity anomaly at 500 km depth require a thermal anomaly of at least 150 K and 220 K, respectively. This reaches the lower limit of the central temperature anomaly of an active mantle plume [e.g., Nolet et al., 2006; Steinberger and Antretter, 2006]. On the other hand, the New England Province has been tectonically inactive for the last ~100 Myr. The Montegonian hot spot passed through this region and created the Montegonian Hills at about 125 Ma [Sleep, 1990]. Hence, the thermal anomaly in this region should be weak at present, if not zero. Therefore, it is hard to explain the large amplitude of the velocity anomaly by a purely thermal effect. This suggests nonthermal origin of the observed slow velocity, possibly including both chemical heterogeneity and the presence of water/partial melt [van der Lee et al., 2008].

4.4. The Colorado Plateau

[38] The SH velocity model shows fast anomalies under the Colorado Plateau at 0–200 km depth (Figure 13, BB'). This high-velocity structure is thicker in the southwest than in the northeast, which is also observed by P wave tomography except with an overall thinner root [Sigloch, 2008]. This uneven thickness is resolved as shown in Figure S8, FF'. These fast anomalies probably represent a thick lithospheric root. Since the 2 km elevation of the Colorado Plateau largely exceeds the elevation that is expected to be supported by depleted cratonic lithosphere, some other form of support, static and/or dynamic, is needed. Various suggestions have been made, including warming of heterogeneous lithosphere [Roy et al., 2009], edge-driven convection [Karlstrom et al., 2008; Van Wijck et al., 2010], dynamic modeling of mantle convection [Moucha et al., 2009; Liu and Gurnis, 2010], and small-scale mantle convection represented by drip-like high-velocity bodies in tomographic images [Schmandt and Humphreys, 2010b]. In our SH velocity model, we observe slow anomalies under southern California and northern Baja California in the lower mantle down to 1000 km depth. These slow anomalies overlap the warm mantle upwelling proposed by Moucha et al. [2009] which is responsible for the uplift in the central Basin and Range Province and Colorado Plateau. The thicker root in the southwest coincides with the higher accumulative dynamic topography in the southwest plateau for the last 25 Myr from the mantle convection model [Moucha et al., 2009].

[39] In the upper mantle, at 100 km depth (Figure 13, BB', map view), anomalies as low as $-6\%$ are observed under the boundary between the Colorado Plateau and the Basin and Range. The large magnitude of the slow anomalies suggest partial melt, as discussed in section 4.2, or the existence of water, which might be a result of hydration of the mantle beneath the Basin and Range due to the subduction of the Farallon slab under this region over 30 Myr ago [Atwater and Stock, 1998]. The slow anomaly rapidly changes to a fast anomaly as we go southeast from the Basin and Range to the Colorado Plateau, with a velocity contrast of 9.0% over 150 km. This large velocity gradient is resolved in our model as shown in Figure S7 (100 km). Sine et al. [2008] propose that this large velocity gradient defines a boundary between altered Paleozoic lithosphere (under the Basin and Range) and unaltered Proterozoic lithosphere (under the Colorado Plateau).

5. The Attenuation Model of the Mantle Beneath North America

[40] A catalog of the attenuation maps is given in Figures S4–S6 (left). These maps show that a large portion of the attenuation signal is located in the western United States, because the attenuation resolution in the central and eastern United States is low (Figure 12) due to poor data coverage (Figures 5e and 6e). Figure S9 shows that the attenuation resolution (especially amplitude recovery) starts to decrease at 600 km depth and the anomalies become unresolvable at 800 km depth and below. In the following, we discuss the relationship between attenuation and velocity anomalies in the upper mantle and transition zone beneath the United States, which may provide extra constraints on the physical sources of mantle heterogeneities.

[41] If we assume an approximate linear relationship $\delta \ln Q_\alpha = k \delta \ln V_S + b$, then the correlation coefficient between $\delta \ln Q_\alpha$ and $\delta \ln V_S$ describes the strength of this linear relationship. Because different physical sources (e.g., temperature, water content, partial melt, chemical composition, grain size) of mantle heterogeneities give different slopes of the linear relationship, a low correlation coefficient suggests coexistence of multiple physical sources. Even the same physical source has a depth-dependent property and thus produces a depth-dependent slope, so we study the correlation coefficient and slope at each depth rather than the average value. Figure 14a plots the variation of the signed correlation coefficient with depth for the western United States (WUS, west of 255°E) and the central and eastern United States (EUS, east of 255°E), respectively. All correlation coefficients are positive, meaning a dominant coexistence of slow (fast) velocity and high (low) attenuation. Such positive correlation is also observed in global
models derived from surface waves [e.g., Romanowicz, 1990; Artemieva et al., 2004; Dalton and Ekström, 2006] and in regional studies [e.g., Roth et al., 2000]. A positive correlation is predicted for the effects of most physical sources, such as temperature [e.g., Karato, 1993; Jackson et al., 2002], water content [e.g., Karato, 2006], partial melt with grain boundary sliding [e.g., Jackson et al., 2004; Faul et al., 2004], and grain size [e.g., Faul and Jackson, 2005]. The large correlation coefficient for EUS suggests one major physical source of attenuation and velocity heterogeneities under EUS, which is most likely temperature [e.g., Shito et al., 2006]. WUS has a lower correlation coefficient than EUS, suggesting that nonthermal sources play a more important role in forming heterogeneities under WUS, especially at the larger depth.

[42] Further insight into the physical state of the mantle comes from examining the variation of the slope \( k = \partial(\delta \ln Q_5)/\partial(\delta \ln V_S) \) with depth (Figure 14b). Because \( \delta \ln Q_5 \) and \( \delta \ln V_S \) do not have a strict linear relationship, we treat them as random variables and estimate the slope as the direction of the major axis of the error ellipse. A formal estimate for the uncertainty in the slope is obtained using a 10% resampling technique (jackknifing [Tian et al., 2009]). Figure 14 shows that small slope uncertainties correspond to large correlation coefficients (e.g., under EUS), and this is expected from the situation of one major physical source. Large slope uncertainties correspond to small correlation coefficients (e.g., around 350 km depth under WUS), and are expected from the coexistence of multiple physical sources. The correlation coefficient at 600 km depth under WUS is so low that a simple linear relationship is no longer sufficient. Therefore we do not discuss the slope at this depth. The slope for EUS mainly reflects the behavior of thermal effects, as discussed above. The slope for WUS is significantly larger than that for EUS, suggesting nonthermal physical sources under WUS that produce larger slopes than temperature, especially around 350 km depth. Such sources are possibly increasing water content [Karato, 2006] and partial melt with grain boundary sliding [Jackson et al., 2004; Faul et al., 2004].

[43] Extra constraints on the physical state of the mantle may be obtained by examining the lateral variation of the \( \delta \ln V_S - \delta \ln Q_5 \) relationship. Figure 15 shows maps of the normalized \( C = \delta \ln V_S \times \delta \ln Q_5 \) in the upper mantle and transition zone under North America. Positive values of \( C \) are dominant, consistent with the observed positive correlation coefficients (Figure 14a). Large-scale positive \( C \) exists in various tectonic regions, e.g., in the Wyoming craton at 100–200 km depth, under the magmatically active Basin and Range at 100–200 km depth, in the subducted slabs under Iowa, Illinois, Missouri at 400–600 km depth. Positive correlation under the old continents and magmatic regions on a global scale is reported by Dalton et al. [2009].

Note that large positive \( C \) does not necessarily indicate a large correlation coefficient, because there may be multiple physical sources with different (but all positive) slopes \( k \), which in combination gives a relatively low (but positive) correlation coefficient. Relatively large-scale anticorrelation between \( \delta \ln V_S \) and \( \delta \ln Q_5 \) (negative \( C \)) is also observed, and one can only speculate about its cause. Low velocity and low attenuation coexist over the northwest coast at 200–400 km depth. This is likely due to the smearing of the slab-related, low-attenuation feature in the attenuation model. The coexistence of low velocity and low attenuation under the Central Valley at 100–400 km depth is more puzzling, though it may perhaps be explained by the effect of partial melt with a melt-squirt mechanism [Hammond and Humphreys, 2000a, 2000b]. A third example of anticorrelation is the coexistence of high velocity and high attenuation under the Northern Rocky Mountains at 100–200 km depth. Calculations show that for natural peridotites, an increase in Mg# significantly increases \( V_S \) [Lee, 2003]. On the other hand, attenuation is
expected to be much less sensitive to major element variations [Karato, 2006].

6. Conclusions

[44] We perform a joint inversion on multiple-frequency \(SH\) wave delays and amplitude anomalies, \(SS\) wave differential delays, and Love wave fundamental mode phase delays, to simultaneously obtain the velocity and attenuation structure under North America. Besides the intrinsic frequency dependence of Love wave phases, frequency dependence is also observed for all the body wave data in our study, indicating the presence of anomalies smaller than the width of the Fresnel zones.

[45] Our \(SH\) velocity model very much confirms the same fast anomalies as in the \(P\) velocity model by Sigloch et al. [2008], including the two separate subduction systems under North America and the slab gap under the western United States. It also reveals further evidence of high-level segmentation and deformation of the slab, including the droplet-like fragments of S2 and F2 in the lower mantle, a tear in F2 under 700 km, and discontinuities around 410 km depth in the slab under the western United States. With the more recent USArray data, we are able to extend the high velocity resolution further east compared with Sigloch et al. [2008] and Tian et al. [2009], and start to see a glimpse of the Yellowstone plume. A lower mantle plume Y2 is observed to originate from about 1500 km depth and to rise up through the slab gap. We propose that a southward mantle flow produces the 40° tilting angle (from vertical) of Y2.

[46] Attenuation is only resolved in the upper mantle and transition zone under the United States. Large positive correlation coefficients between \(\delta \ln V_s\) and \(\delta \ln Q_s\) are observed under the central and eastern United States, suggesting one major physical source of mantle heterogeneities, most likely temperature. Smaller correlation coefficients and larger \(\delta \ln Q_s - \delta \ln V_s\) slopes are observed under the western United States, suggesting that nonthermal physical sources, probably the existence of water and partial melt (with grain boundary sliding), are playing a more important role, especially around 350 km depth. Anticorrelation is observed...
in the upper mantle under the Central Valley and the Northern Rocky Mountains.

The inclusion of Love wave phase delays helps improve velocity resolution in the lower mantle by better constraining the upper mantle. It also influences the attenuation image indirectly by changing the velocity image and thus the focusing effect, resulting in weaker attenuation anomalies above 200 km and stronger attenuation anomalies below 500 km. The misfits of Love wave and SS wave data are larger than those of SH wave data.

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References

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